

Package ‘rsq’

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Title R-Squared and Related Measures

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Imports methods, stats, MASS, lme4, nlme, Deriv, Matrix, deming

Suggests

Description

Calculate generalized R-squared, partial R-squared, and partial correlation coefficients for generalized linear (mixed) models (including quasi models with well defined variance functions).

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NeedsCompilation no

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hcrabs	<i>Satellites of Female Horseshoe Crabs</i>
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Description

Recorded are the numbers of male satellites, and other characteristics of 173 female horseshoe crabs.

Usage

```
data("hcrabs")
```

Format

A data frame with 173 observations on the following 5 variables.

`color` the female crab's color, coded 1: light; 2: medium light; 3: medium; 4: medium dark; 5: dark. Not all of these colors appear.

`spine` the female crab's spine condition, coded 1: both good; 2: one worn or broken; 3: both worn or broken.

`width` the female crab's carapace width (cm).

`num.satellites` the number of satellite males.

`weight` the female crab's weight (kg).

Details

A nesting female horseshoe crab may have male crabs residing nearby, called satellites, besides the male crab residing in her nest. Brockmann (1996) investigated factors (including the female crab's color, spine condition, weight, and carapace width) which may influence the presence/absence of satellite males. This data set has been discussed by Agresti (2002).

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

Source

Agresti, A. (2012). *An Introduction to Categorical Data Analysis*, 3rd edition. Wiley: New Jersey.

References

Brockmann, H. J. (1996). Satellite male groups in horseshoe crabs. *Limulus polyphemus*. *Ethology*, 102: 1-21.

See Also

[rsq](#), [rsq.partial](#), [pcor](#), [singlm](#).

Examples

```
data(hcrabs)
summary(hcrabs)
head(hcrabs)

attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq(bnfit)
rsq(bnfit,adj=TRUE)
rsq.partial(bnfit)

quasips <- glm(num.satellites~color+spine+width+weight,family=quasipoisson)
rsq(quasips)
rsq(quasips,adj=TRUE)
rsq.partial(quasips)
```

hschool

Attendance Behavior of High School Juniors

Description

Recorded are the number of days of absence, gender, and two test scores of 316 high school juniors from two urban high schools.

Usage

```
data("hschool")
```

Format

A data frame with 316 observations on the following 5 variables.

`school` school of the two, coded 1 or 2;

`male` whether the student is male, coded 1: male; 0: female;

`math` the standardized test score for math;

`langarts` the standardized test score for language arts;

`daysabs` the number of days of absence.

Details

Some school administrators studied the attendance behavior of high school juniors at two schools. Predictors of the number of days of absence include gender of the student and standardized test scores in math and language arts. The original source of this data set is unknown.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

Source

UCLA IDRE Statistical Consulting Group for data analysis.

See Also

[rsq](#), [rsq.partial](#), [pcor](#), [singlm](#).

Examples

```
data(hschool)
summary(hschool)
head(hschool)

require(MASS)
absfit <- glm.nb(daysabs~school+male+math+langarts,data=hschool)
summary(absfit)
rsq(absfit)
rsq(absfit,adj=TRUE)

rsq.partial(absfit)
```

lifetime

Lifetimes in Two Different Environments.

Description

There are 27 tests in each of the two environments.

Usage

```
data("lifetime")
```

Format

A data frame with 54 observations on the following 2 variables.

time the lifetime (x10).

env the environment of each test (kg/mm²).

Details

This data set is discussed by Wang et al. (1992).

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

Source

Wang, H., Ma, B., and Shi, J. (1992). Estimation of environmental factors for the inverse gaussian distribution. *Microelectron. Reliab.*, 32: 931-934.

See Also

[rsq](#), [rsq.partial](#), [pcor](#), [simglm](#).

Examples

```
data(lifetime)
summary(lifetime)
head(lifetime)

attach(lifetime)
igfit <- glm(time~env, family=inverse.gaussian)
rsq(igfit)
rsq(igfit, adj=TRUE)
```

pcor

Partial Correlation for Generalized Linear Models

Description

Calculate the partial correlation for both linear and generalized linear models.

Usage

```
pcor(objF, objR=NULL, adj=FALSE, type=c('v', 'k1', 'sse', 'lr', 'n'))
```

Arguments

objF	an object of class "lm" or "glm", a result of a call to lm , glm , or glm.nb to fit the full model.
objR	an object of class "lm" or "glm", a result of a call to lm , glm , or glm.nb to fit the reduced model.
adj	logical; if TRUE, calculate the adjusted partial R ² .

type the type of R-squared used:

- 'v' (default) – variance-function-based (Zhang, 2016), calling [rsq.v](#);
- 'kl' – KL-divergence-based (Cameron and Windmeijer, 1997), calling [rsq.kl](#);
- 'sse' – SSE-based (Efron, 1978), calling [rsq.sse](#);
- 'lr' – likelihood-ratio-based (Maddala, 1983; Cox and Snell, 1989; Magee, 1990), calling [rsq.lr](#);
- 'n' – corrected version of 'lr' (Nagelkerke, 1991), calling [rsq.n](#).

Details

When the fitting object of the reduced model is not specified, the partial correlation of each covariate (excluding factor covariates with more than two levels) in the model will be calculated.

Value

The partial correlation coefficient is returned.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Cameron, A. C. and Windmeijer, A. G. (1997) An R-squared measure of goodness of fit for some common nonlinear regression models. *Journal of Econometrics*, 77: 329-342.
- Cox, D. R. and Snell, E. J. (1989) *The Analysis of Binary Data*, 2nd ed. London: Chapman and Hall.
- Efron, B. (1978) Regression and ANOVA with zero-one data: measures of residual variation. *Journal of the American Statistical Association*, 73: 113-121.
- Maddala, G. S. (1983) *Limited-Dependent and Qualitative Variables in Econometrics*. Cambridge University.
- Magee, L. (1990) R² measures based on Wald and likelihood ratio joint significance tests. *The American Statistician*, 44: 250-253.
- Nagelkerke, N. J. D. (1991) A note on a general definition of the coefficient of determination. *Biometrika*, 78: 691-692.
- Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.

See Also

[rsq](#), [rsq.partial](#).

Examples

```

data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.partial(bnfit)

bnfitr <- glm(y~color+weight,family=binomial)
rsq.partial(bnfit,bnfitr)

quasibn <- glm(y~color+spine+width+weight,family=quasibinomial)
rsq.partial(quasibn)

quasibnr <- glm(y~color+weight,family=binomial)
rsq.partial(quasibn,quasibnr)

```

rsq

*R-Squared for Generalized Linear (Mixed) Models***Description**

Calculate the coefficient of determination, aka R^2 , for both linear and generalized linear (mixed) models.

Usage

```
rsq(fitObj,adj=FALSE,type=c('v','kl','sse','lr','n'))
```

Arguments

fitObj	an object of class "lm", "glm", "merMod", "lmerMod", or "lme"; usually a result of a call to <code>lm</code> , <code>glm</code> , <code>glm.nb</code> , <code>lmer</code> or <code>glmer</code> or <code>glmer.nb</code> in <code>lme4</code> , or <code>lme</code> in <code>nlme</code> .
adj	logical; if TRUE, calculate the adjusted R^2 .
type	the type of R-squared (only applicable for generalized linear models): <ul style="list-style-type: none"> 'v' (default) – variance-function-based (Zhang, 2017), calling <code>rsq.v</code>; 'kl' – KL-divergence-based (Cameron and Windmeijer, 1997), calling <code>rsq.kl</code>; 'sse' – SSE-based (Efron, 1978), calling <code>rsq.sse</code>; 'lr' – likelihood-ratio-based (Maddala, 1983; Cox and Snell, 1989; Magee, 1990), calling <code>rsq.lr</code>; 'n' – corrected version of 'lr' (Nagelkerke, 1991), calling <code>rsq.n</code>.

Details

Calculate the R-squared for (generalized) linear models. For (generalized) linear mixed models, there are three types of R^2 calculated on the basis of observed response values, estimates of fixed effects, and variance components, i.e., model-based R_M^2 (proportion of variation explained by the model in total, including both fixed-effects and random-effects factors), fixed-effects R_F^2 (proportion of variation explained by the fixed-effects factors), and random-effects R_R^2 (proportion of variation explained by the random-effects factors).

Value

The R^2 or adjusted R^2 . For (generalized) linear mixed models,

R_M^2	proportion of variation explained by the model in total, including both fixed-effects and random-effects factors.
R_F^2	proportion of variation explained by the fixed-effects factors.
R_R^2	proportion of variation explained by the random-effects factors.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Cameron, A. C. and Windmeijer, A. G. (1997) An R-squared measure of goodness of fit for some common nonlinear regression models. *Journal of Econometrics*, 77: 329-342.
- Cox, D. R. and Snell, E. J. (1989) *The Analysis of Binary Data*, 2nd ed. London: Chapman and Hall.
- Efron, B. (1978) Regression and ANOVA with zero-one data: measures of residual variation. *Journal of the American Statistical Association*, 73: 113-121.
- Maddala, G. S. (1983) *Limited-Dependent and Qualitative Variables in Econometrics*. Cambridge University.
- Magee, L. (1990) R^2 measures based on Wald and likelihood ratio joint significance tests. *The American Statistician*, 44: 250-253.
- Nagelkerke, N. J. D. (1991) A note on a general definition of the coefficient of determination. *Biometrika*, 78: 691-692.
- Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.
- Zhang, D. (2020). Coefficients of determination for generalized linear mixed models. *Technical Report*, 20-01, Department of Statistics, Purdue University.

See Also

[rsq.partial](#), [pcor](#), [singlm](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq(bnfit)
rsq(bnfit,adj=TRUE)

quasibn <- glm(y~color+spine+width+weight,family=quasibinomial)
rsq(quasibn)
rsq(quasibn,adj=TRUE)
```



```

psfit <- glm(num.satellites~color+spine+width+weight,family=poisson)
rsq(psfit)
rsq(psfit,adj=TRUE)

quasips <- glm(num.satellites~color+spine+width+weight,family=quasipoisson)
rsq(quasips)
rsq(quasips,adj=TRUE)

# Linear mixed models
require(lme4)
lmm1 <- lmer(Reaction~Days+(Days|Subject),data=sleepstudy)
rsq(lmm1)
rsq.lmm(lmm1)

# Generalized linear mixed models
data(cbpp)
glmm1 <- glmer(cbind(incidence,size-incidence)~period+(1|herd),data=cbpp,family=binomial)
rsq(glmm1)

```

rsq.glmm

R-Squared for Generalized Linear Mixed Models

Description

Calculate the variance-function-based R-squared for generalized linear mixed models.

Usage

```
rsq.glmm(fitObj,adj=FALSE)
```

Arguments

fitObj	an object of class "glmerMod", usually, a result of a call to glmer or glmer.nb in lme4 .
adj	logical; if TRUE, calculate the adjusted R ² .

Details

There are three types of R² calculated on the basis of observed response values, estimates of fixed effects, and variance components, i.e., model-based R_M² (proportion of variation explained by the model in total, including both fixed-effects and random-effects factors), fixed-effects R_F² (proportion of variation explained by the fixed-effects factors), and random-effects R_R² (proportion of variation explained by the random-effects factors).

Value

R_M^2	proportion of variation explained by the model in total, including both fixed-effects and random-effects factors.
R_F^2	proportion of variation explained by the fixed-effects factors.
R_R^2	proportion of variation explained by the random-effects factors.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.
- Zhang, D. (2020). Coefficients of determination for mixed-effects models. arXiv:2007.08675.

See Also

[vresidual](#), [rsq](#), [rsq.v](#).

Examples

```
require(lme4)
data(cbpp)
glmm1 <- glmer(cbind(incidence, size-incidence)~period+(1|herd), data=cbpp, family=binomial)
rsq.glm(glmm1)
rsq(gLmm1)
```

rsq.kl

KL-Divergence-Based R-Squared

Description

The Kullback-Leibler-divergence-based R^2 for generalized linear models.

Usage

```
rsq.kl(fitObj, adj=FALSE)
```

Arguments

fitObj	an object of class "lm" or "glm", usually, a result of a call to lm , glm , or glm.nb .
adj	logical; if TRUE, calculate the adjusted R^2 .

Details

This version of R^2 was proposed by Cameron and Windmeijer (1997). It is extended to quasi models (Zhang, 2017) based on the quasi-likelihood function (McCullagh, 1983).

Value

The R^2 or adjusted R^2 .

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

Cameron, A. C. and Windmeijer, A. G. (1997) An R-squared measure of goodness of fit for some common nonlinear regression models. *Journal of Econometrics*, 77: 329-342.

McCullagh, P. (1983) Quasi-likelihood functions. *Annals of Statistics*, 11: 59-67.

See Also

[rsq](#), [rsq.partial](#), [pcor](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.kl(bnfit)
rsq.kl(bnfit,adj=TRUE)

psfit <- glm(num.satellites~color+spine+width+weight,family=poisson)
rsq.kl(psfit)
rsq.kl(psfit,adj=TRUE)

# Effectiveness of Bicycle Safety Helmets in Thompson et al. (1989)
y <- matrix(c(17,218,233,758),2,2)
x <- factor(c("yes","no"))
tbn <- glm(y~x,family=binomial)
rsq.kl(tbn)
rsq.kl(tbn,adj=TRUE)
```

rsq.lmm

R-Squared for Linear Mixed Models

Description

Calculate the R-squared for linear mixed models.

Usage

```
rsq.lmm(fitObj,adj=FALSE)
```

Arguments

<code>fitObj</code>	an object of class "merMod" or "lmerMod" or "lme", usually, a result of a call to <code>lmer</code> in <code>lme4</code> , or <code>lme</code> in <code>nlme</code> .
<code>adj</code>	logical; if TRUE, calculate the adjusted R^2 .

Details

There are three types of R^2 calculated on the basis of observed response values, estimates of fixed effects, and variance components, i.e., model-based R_M^2 (proportion of variation explained by the model in total, including both fixed-effects and random-effects factors), fixed-effects R_F^2 (proportion of variation explained by the fixed-effects factors), and random-effects R_R^2 (proportion of variation explained by the random-effects factors).

Value

R_M^2	proportion of variation explained by the model in total, including both fixed-effects and random-effects factors.
R_F^2	proportion of variation explained by the fixed-effects factors.
R_R^2	proportion of variation explained by the random-effects factors.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

Zhang, D. (2020). Coefficients of determination for mixed-effects models. arXiv:2007.0867.

See Also

[rsq](#), [rsq.v](#).

Examples

```
# lmer in lme4
require(lme4)
lmm1 <- lmer(Reaction~Days+(Days|Subject), data=sleepstudy)
rsq(lmm1)
rsq.lmm(lmm1)

# lme in nlme
require(nlme)
lmm2 <- lme(Reaction~Days, data=sleepstudy, random=~Days|Subject)
rsq(lmm2)
rsq.lmm(lmm2)
```

`rsq.lr`*Likelihood-Ratio-Based R-Squared*

Description

Calculate the likelihood-ratio-based R^2 for generalized linear models.

Usage

```
rsq.lr(fitObj,adj=FALSE)
```

Arguments

`fitObj` an object of class "lm" or "glm", usually, a result of a call to [lm](#), [glm](#), or [glm.nb](#).
`adj` logical; if TRUE, calculate the adjusted R^2 .

Details

Proposed by Maddala (1983), Cox and Snell (1989), and Magee (1990), this version of R^2 is defined with the likelihood ratio statistics, so it is not defined for quasi models. It reduces to the classical R^2 when the variance function is constant or linear.

Value

The R^2 or adjusted R^2 .

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Cox, D. R. and Snell, E. J. (1989) *The Analysis of Binary Data*, 2nd ed. London: Chapman and Hall.
- Maddala, G. S. (1983) *Limited-Dependent and Qualitative Variables in Econometrics*. Cambridge University.
- Magee, L. (1990) R^2 measures based on Wald and likelihood ratio joint significance tests. *The American Statistician*, 44: 250-253.

See Also

[rsq](#), [rsq.partial](#), [pcor](#), [rsq.n](#).

Examples

```

data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.lr(bnfit)
rsq.lr(bnfit,adj=TRUE)

psfit <- glm(num.satellites~color+spine+width+weight,family=poisson)
rsq.lr(psfit)
rsq.lr(psfit,adj=TRUE)

# Effectiveness of Bycycle Safety Helmets in Thompson et al. (1989)
y <- matrix(c(17,218,233,758),2,2)
x <- factor(c("yes","no"))
tbn <- glm(y~x,family=binomial)
rsq.lr(tbn)
rsq.lr(tbn,adj=TRUE)

```

rsq.n

*Corrected Likelihood-Ratio-Based R-Squared***Description**

Corrected likelihood-ratio-based R^2 for generalized linear models.

Usage

```
rsq.n(fitObj,adj=FALSE)
```

Arguments

`fitObj` an object of class "lm" or "glm", usually, a result of a call to `lm`, `glm`, or `glm.nb`.
`adj` logical; if TRUE, calculate the adjusted R^2 .

Details

Nagelkerke (1991) proposed this version of R^2 to correct the likelihood-ratio-statistic-based one which was proposed by Maddala (1983), Cox and Snell (1989), and Magee (1990). This corrected generalization of R^2 cannot reduce to the classical R^2 in case of linear models. It is not defined for quasi models.

Value

The R^2 or adjusted R^2 .

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Cox, D. R. and Snell, E. J. (1989) *The Analysis of Binary Data*, 2nd ed. London: Chapman and Hall.
- Maddala, G. S. (1983) *Limited-Dependent and Qualitative Variables in Econometrics*. Cambridge University.
- Magee, L. (1990) R² measures based on Wald and likelihood ratio joint significance tests. *The American Statistician*, 44: 250-253.
- Nagelkerke, N. J. D. (1991) A note on a general definition of the coefficient of determination. *Biometrika*, 78: 691-692.

See Also

[rsq](#), [rsq.partial](#), [pcor](#), [rsq.lr](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.n(bnfit)
rsq.n(bnfit,adj=TRUE)

psfit <- glm(num.satellites~color+spine+width+weight,family=poisson)
rsq.n(psfit)
rsq.n(psfit,adj=TRUE)

# Effectiveness of Bycycle Safety Helmets in Thompson et al. (1989)
y <- matrix(c(17,218,233,758),2,2)
x <- factor(c("yes","no"))
tbn <- glm(y~x,family=binomial)
rsq.n(tbn)
rsq.n(tbn,adj=TRUE)
```

rsq.partial

Partial R-Squared for Generalized Linear Models

Description

Calculate the coefficient of partial determination, aka partial R², for both linear and generalized linear models.

Usage

```
rsq.partial(objF,objR=NULL,adj=FALSE,type=c('v','kl','sse','lr','n'))
```

Arguments

objF	an object of class "lm" or "glm", a result of a call to <code>lm</code> , <code>glm</code> , or <code>glm.nb</code> to fit the full model.
objR	an object of class "lm" or "glm", a result of a call to <code>lm</code> , <code>glm</code> , or <code>glm.nb</code> to fit the reduced model.
adj	logical; if TRUE, calculate the adjusted partial R^2 .
type	the type of R-squared: 'v' (default) – variance-function-based (Zhang, 2016), calling <code>rsq.v</code> ; 'kl' – KL-divergence-based (Cameron and Windmeijer, 1997), calling <code>rsq.kl</code> ; 'sse' – SSE-based (Efron, 1978), calling <code>rsq.sse</code> ; 'lr' – likelihood-ratio-based (Maddala, 1983; Cox and Snell, 1989; Magee, 1990), calling <code>rsq.lr</code> ; 'n' – corrected version of 'lr' (Nagelkerke, 1991), calling <code>rsq.n</code> .

Details

When the fitting object of the reduced model is not specified, the partial R^2 of each term in the model will be calculated.

Value

Returned values include `adjustment` and `partial.rsq`. When `objR` is not NULL, `variable.full` and `variable.reduced` are returned; otherwise `variable` is returned.

<code>adjustment</code>	logical; if TRUE, calculate the adjusted partial R^2 .
<code>variable.full</code>	all covariates in the full model.
<code>variable.reduced</code>	all covariates in the reduced model.
<code>variable</code>	all covariates in the full model.
<code>partial.rsq</code>	partial R^2 or the adjusted partial R^2 .

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Cameron, A. C. and Windmeijer, A. G. (1997) An R-squared measure of goodness of fit for some common nonlinear regression models. *Journal of Econometrics*, 77: 329-342.
- Cox, D. R. and Snell, E. J. (1989) *The Analysis of Binary Data*, 2nd ed. London: Chapman and Hall.
- Efron, B. (1978) Regression and ANOVA with zero-one data: measures of residual variation. *Journal of the American Statistical Association*, 73: 113-121.
- Maddala, G. S. (1983) *Limited-Dependent and Qualitative Variables in Econometrics*. Cambridge University.

Magee, L. (1990) R^2 measures based on Wald and likelihood ratio joint significance tests. *The American Statistician*, 44: 250-253.

Nagelkerke, N. J. D. (1991) A note on a general definition of the coefficient of determination. *Biometrika*, 78: 691-692.

Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.

See Also

[rsq](#), [pcor](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.partial(bnfit)

bnfitr <- glm(y~color+weight,family=binomial)
rsq.partial(bnfit,bnfitr)

quasibn <- glm(y~color+spine+width+weight,family=quasibinomial)
rsq.partial(quasibn)

quasibnr <- glm(y~color+weight,family=binomial)
rsq.partial(quasibn,quasibnr)
```

rsq.sse

SSE-Based R-Squared

Description

The sum-of-squared-errors-based R^2 for generalized linear models.

Usage

```
rsq.sse(fitObj,adj=FALSE)
```

Arguments

`fitObj` an object of class "lm" or "glm", usually, a result of a call to [lm](#), [glm](#), or [glm.nb](#).
`adj` logical; if TRUE, calculate the adjusted R^2 .

Details

This version of R^2 was proposed by Efron (1978). It is calculated on the basis of the formula of the classical R^2 .

Value

The R^2 or adjusted R^2 .

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

Efron, B. (1978) Regression and ANOVA with zero-one data: measures of residual variation. *Journal of the American Statistical Association*, 73: 113-121.

See Also

[rsq](#), [rsq.partial](#), [pcor](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.sse(bnfit)
rsq.sse(bnfit,adj=TRUE)

psfit <- glm(num.satellites~color+spine+width+weight,family=poisson)
rsq.sse(psfit)
rsq.sse(psfit,adj=TRUE)

# Effectiveness of Bycycle Safety Helmets in Thompson et al. (1989)
y <- matrix(c(17,218,233,758),2,2)
x <- factor(c("yes","no"))
tbn <- glm(y~x,family=binomial)
rsq.sse(tbn)
rsq.sse(tbn,adj=TRUE)
```

rsq.v

Variance-Function-Based R-Squared

Description

Calculate the variance-function-based R-squared for generalized linear (mixed) models.

Usage

```
rsq.v(fitObj,adj=FALSE)
```

Arguments

<code>fitObj</code>	an object of class "lm", "glm", "lme", or "glmerMod", usually, a result of a call to lm , glm , glm.nb , glmer , or glmer.nb .
<code>adj</code>	logical; if TRUE, calculate the adjusted R^2 .

Details

The R^2 relies on the variance function, and is well-defined for quasi models. It reduces to the classical R^2 when the variance function is constant or linear. For (generalized) linear mixed models, there are three types of R^2 calculated on the basis of observed response values, estimates of fixed effects, and variance components, i.e., model-based R_M^2 (proportion of variation explained by the model in total, including both fixed-effects and random-effects factors), fixed-effects R_F^2 (proportion of variation explained by the fixed-effects factors), and random-effects R_R^2 (proportion of variation explained by the random-effects factors).

Value

The R^2 or adjusted R^2 . For (generalized) linear mixed models,

R_M^2	proportion of variation explained by the model in total, including both fixed-effects and random-effects factors.
R_F^2	proportion of variation explained by the fixed-effects factors.
R_R^2	proportion of variation explained by the random-effects factors.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

- Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.
- Zhang, D. (2020). Coefficients of determination for mixed-effects models. arXiv:2007.08675.

See Also

[vresidual](#), [rsq](#), [rsq.glmm](#), [rsq.partial](#), [pcor](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family=binomial)
rsq.v(bnfit)
rsq.v(bnfit,adj=TRUE)

quasibn <- glm(y~color+spine+width+weight,family=quasibinomial)
rsq.v(quasibn)
```

```
rsq.v(quasibn,adj=TRUE)

# Generalized linear mixed models
require(lme4)
data(cbpp)
glmm1 <- glmer(cbind(incidence,size-incidence)~period+(1|herd),data=cbpp,family=binomial)
rsq.v(glmm1)
```

simglm

Simulate Data from Generalized Linear Models

Description

Simulate data from linear and generalized linear models. Only the first covariate truly affects the response variable with coefficient equal to lambda.

Usage

```
simglm(family=c("binomial", "gaussian", "poisson", "Gamma"),lambda=3,n=50,p=3)
```

Arguments

family	the family of the distribution.
lambda	size of the coefficient of the first covariate.
n	the sample size.
p	the number of covarites.

Details

The first covariate takes 1 in half of the observations, and 0 or -1 in the other half. When lambda gets larger, it is supposed to easier to predict the response variable.

Value

Returned values include yx and beta.

yx	a data frame including the response y and covariates x.1, x.2, and so on.
beta	true values of the regression coefficients.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.

See Also

[rsq](#), [rsq.partial](#), [pcor](#).

Examples

```
# Poisson Models
sdata <- simglm(family="poisson",lambda=4)
fitf <- glm(y~x.1+x.2+x.3,family=poisson,data=sdata$yx)
rsq(fitf) # type='v'

fitr <- glm(y~x.2+x.3,family=poisson,data=sdata$yx)
rsq(fitr) # type='v'
rsq(fitr,type='kl')
rsq(fitr,type='lr')
rsq(fitr,type='n')

pcor(fitr) # type='v'
pcor(fitr,type='kl')
pcor(fitr,type='lr')
pcor(fitr,type='n')

# Gamma models with shape=100
n <- 50
sdata <- simglm(family="Gamma",lambda=4,n=n)
fitf <- glm(y~x.1+x.2+x.3,family=Gamma,data=sdata$yx)
rsq(fitf) # type='v'
rsq.partial(fitf) # type='v'

fitr <- glm(y~x.2,family=Gamma,data=sdata$yx)
rsq(fitr) # type='v'
rsq(fitr,type='kl')
rsq(fitr,type='lr')
rsq(fitr,type='n')

# Likelihood-ratio-based R-squared
y <- sdata$yx$y
yhatr <- fitr$fitted.values
fit0 <- update(fitr,~1)
yhat0 <- fit0$fitted.values
llr <- sum(log(dgamma(y,shape=100,scale=yhatr/100)))
ll0 <- sum(log(dgamma(y,shape=100,scale=yhat0/100)))

# Likelihood-ratio-based R-squared
1-exp(-2*(llr-ll0)/n)

# Corrected likelihood-ratio-based R-squared
(1-exp(-2*(llr-ll0)/n))/(1-exp(-2*ll0/n))
```

Description

Simulate data from linear and generalized linear mixed models. The coefficients of the two covariate are specified by beta.

Usage

```
simglm(family=c("binomial", "gaussian", "poisson", "negative.binomial"),
beta=c(2, 0), tau=1, n=200, m=10, balance=TRUE)
```

Arguments

family	the family of the distribution.
beta	regression coefficients (excluding the intercept which is set as zero).
tau	the variance of the random intercept.
n	the sample size.
m	the number of groups.
balance	simulate balanced data if TRUE, unbalanced data otherwise.

Details

The first covariate takes 1 in half of the observations, and 0 or -1 in the other half. When beta gets larger, it is supposed to be easier to predict the response variable.

Value

Returned values include yx, beta, and u.

yx	a data frame including the response y and covariates x1, x2, and so on.
beta	true values of the regression coefficients.
u	the random intercepts.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

Zhang, D. (2020). Coefficients of determination for generalized linear mixed models. *Technical Report*, 20-01, Department of Statistics, Purdue University.

See Also

[rsq](#), [rsq.lmm](#), [rsq.glmm](#), [simglm](#),

Examples

```
require(lme4)

# Linear mixed models
gdata <- simglmm(family="gaussian")
lmm1 <- lmer(y~x1+x2+(1|subject),data=gdata$yx)
rsq(lmm1)

# Generalized linear mixed models
bdata <- simglmm(family="binomial",n=400,m=20)
glmm1 <- glmer(y~x1+x2+(1|subject),family="binomial",data=bdata$yx)
rsq(glmm1)
```

toxox

Toxoplasmosis Test in El Salvador

Description

Recorded are the numbers of subjects testing positive for toxoplasmosis in 34 cities of El Salvador.

Usage

```
data("toxox")
```

Format

A data frame with the test results in 34 cities of El Salvador, including the following 4 variables.

city index of each city.

positive the number of subjects testing positive for toxoplasmosis.

nsubs the total number of subjects tested.

rainfall annual rainfall (mm) in home city of subject.

Details

All subjects are between 11 and 15 year old. The data set was abstracted from a larger data set in Rmington et al. (1970).

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

Source

Efron, B. (1978). Regression and ANOVA with zero-one data: measures of residual variation. *JASA*, 73: 113-121.

References

Remington, J.S., Efron, B., Cavanaugh, E., Simon, H.J., and Trejos, A. (1970). Studies on toxoplasmosis in El Salvador, prevalence and incidence of toxoplasmosis as measured by the Sabin-Feldman Dye test. *Transactions of the Royal Society of Tropical Medicine and Hygiene*, 64: 252-267.

See Also

[rsq](#), [rsq.partial](#), [pcor](#), [simglm](#).

Examples

```
data(toxo)
summary(toxo)
attach(toxo)

toxofit<-glm(cbind(positive, nsubs-positive)~rainfall+I(rainfall^2)+I(rainfall^3), family=binomial)

rsq(toxofit)
rsq(toxofit, adj=TRUE)
rsq.partial(toxofit)

detach(toxo)
```

vresidual

Variance-Function-Based Residuals

Description

Calculate the variance-function-based residuals for generalized linear models, which are used to calculate the variance-function-based R-squared.

Usage

```
vresidual(y, yfit, family=binomial(), variance=NULL)
```

Arguments

y	a vector of observed values.
yfit	a vector of fitted values.
family	family of the distribution.
variance	variance function (specified by family by default).

Details

The calculated residual relies on the variance function, and is well-defined for quasi models. It reduces to the classical residual when the variance function is constant or linear. Note that only the variance function is required to specify, via either "family" or "variance".

Value

Variance-function-based residuals.

Author(s)

Dabao Zhang, Department of Statistics, Purdue University

References

Zhang, D. (2017). A coefficient of determination for generalized linear models. *The American Statistician*, 71(4): 310-316.

See Also

[rsq.v](#), [rsq](#).

Examples

```
data(hcrabs)
attach(hcrabs)
y <- ifelse(num.satellites>0,1,0)
bnfit <- glm(y~color+spine+width+weight,family="binomial")
vresidual(y,bnfit$fitted.values,family="binomial")

# Effectiveness of Bicycle Safety Helmets in Thompson et al. (1989)
y <- matrix(c(17,218,233,758),2,2)
x <- factor(c("yes","no"))
tbn <- glm(y~x,family="binomial")
yfit <- cbind(tbn$fitted.values, 1-tbn$fitted.values)
vr0 <- vresidual(matrix(0,2,1),yfit[,1],family="binomial")
vr1 <- vresidual(matrix(1,2,1),yfit[,2],family="binomial")
y[,1]*vr0+y[,2]*vr1
```

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