micsr objects

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micsr provides a special micsr class for fitted models, that is particularly convenient for models fitted by maximum likelihood.

Estimation

With **micsr**, models are estimated using the **micsr::maximize** function which is an interface for three optimization routines, selected using the **opt** argument:

- "bfgs" uses the stats::optim function with the method argument set to "BFGS",
- "nlm" uses the stats::nlm function which uses the Newton-Ralphson algorithm,
- "newton" uses the micsr::newton function which is a fast implementation of the Newton-Ralphson algorithm.

For simple log-likelihood function, "newton" is the fastest way to estimate the model, otherwise, "bfgs" is the safer.

The first argument is the function that returns the log-likelihood of the model and further argument of this function can be passed using the ... argument of maximize:

- gradient, hessian and information are booleans which enable to compute the gradient, the hessian and the information matrix that are returned as attributes of the result,
- sum is a boolean: if FALSE the result is a vector containing the individual contributions to the log-likelihood and the gradient attribute is a matrix containing the individual contributions to elements of the gradients,
- opposite is a boolean: if TRUE, the opposite of the function, the gradient and the hessian are returned; this is useful if the optimization function performs a minimization,
- y, X and weights are the vector of response, the matrix of covariates and a vector of weights.

Several functions are provided to estimate models already available in core \mathbf{R} (the stats package) and recommended package.

- binomreg can be used to estimate the binomial model as an alternative to stats::glm function. An "identity" link is provided to estimate the linear probability model and two-part formulas can be provided to estimate the probit model with instrumental variables. In this case, several method of estimation are provided selected by the method argument: either "ml" for maximum-likelihood, "twosteps" for the two-step estimator and "minchisq" for the minimum χ^2 estimator,
- poisreg estimates different flavors of count models. The basic use of this function estimate the Poisson model as an alternative to the stats::glm function with family = poisson(link = 'log'). Mixing distribution can be introduced with the mixing argument which is "none" by default but can be set to "lognorm" to get the log-normal Poisson model and to "gamma" to get the NegBin model (the vlink argument is either set to "nb1" or to "nb2" to get the two flavors of the NegBin model, which can also be estimated using the MASS::glm.nb function),
- weibreg estimates the Weibull model that is normally estimated using the survival::survreg function with the default "weibull" dist argument. Using the model argument, one can use the "accelerated failure time" ("aft") or the "proportional hazard" parametrization ("ph"). Moreover, the most used mixing survival model is obtained by setting the mixing argument to TRUE (in this case, the gamma mixing distribution is used).
- ordreg estimates the ordered model, also called, for the logit link the "proportional odds logistic regression). A link argument enables to estimate the model with a probit, logit or cloglog link. This model can be estimated using the MASS::polr function but ordreg deals with censored responses.
- tobit1 estimates models for truncated responses, using either censored or truncated samples (using the sample argument); in the first case we get the so-called tobit or to-bit1 model, in the second case the truncated model. The left and right arguments can be set to indicate the truncation points (the convenient default is 0 for the former and +∞ for the latter). Several methods of estimations are provided and selected using the method arguments: "ml" for maximum likelihood, "lm" for the (biased) linear estimator, "twostep" for the two-steps consistent estimator and "trimmed" for the symmetric trimmed estimator. If a two-part formula is provided, by default, an instrumental variable is performed, either using maximum likelihood or the minimum χ² estimator. If the scedas argument is not null, but set either to "exp" or "pnorm", the heterosckedastic tobit model is estimated.

All these functions have in common with stats::lm their first arguments: formula, data, subset, weights, na.action, offset and contrasts. Supplementary arguments include opt, maxit and trace to select the optimization method with a given maximum number of iterations and level of printing, start to indicate a vector of starting values and check_gradient to check the correspondence between the analytical and the numerical gradients.

The returned objects, of class micsr includes:

• coefficients: the vector of coefficients,

- model: the model frame,
- terms: model terms,
- value: a vector of individual contribution to the log-likelihood,
- gradient: the matrix of individual contributions to the gradient, also called the estimating function,
- hessian: the hessian
- info: the estimation of the information matrix
- fitted.values: a vector of fitted values,
- linear.predictors: a vector of linear predictors, i.e., $X\hat{\beta}$
- logLik: a vector of length three containing the log-likelihood for the proposed, the saturated and the null models,
- tests: a vector of length three containing the three tests (the Wald, the score and the likelihood ratio tests) that "all the coefficients except the intercept are zero" (the equivalent of the F test for the linear model); these statistics can be used to compute different flavors of the coefficient of determination,
- df.residual: the number of fitted coefficients,
- **npar**: a named numeric vector, the names being the name of the group of coefficients and the value the number of parameter in the group,
- est_method: a character indicating the method of estimation, i.e., ml or twostep,
- call, na.action, weights, offset, contrasts and xlevels (as in lm objects),
- family a family object (as in glm),
- check_gradient: if the check_gradient argument is TRUE, the result is a list containing, for the gradient and the hessian, the maximal absolute value of the difference between the analytical and the numerical gradient and hessian; attribute "gradient" is a matrix containing the numerical and the analytical gradient and attributes "anal_hess" and "num_hess" contain the analytical and the numerical hessians.

Subsets of coefficients

Often, especially for advanced models, the whole set of fitted parameters can be splitted in several groups. For example, while fitted by maximum likelihood a limited dependent model (probit or tobit):

fitted coefficients belongs to 4 different groups:

• the coefficients associated with covariates (the coefficients of main interest,

- the coefficients of the residuals of the endogenous variables,
- the coefficients of the instruments,
- the parameters of the cholesky decomposition of the covariance matrix for the endogenous variables.

This information is stored in the npar element of the micsr object:

```
bank_msq$npar
covariates resid instruments chol
6 2 14 3
attr(,"default")
[1] "covariates" "resid"
```

It's a named list of integers containing the number of coefficients for each groups, in their order of appearance in the coefficient element of the micsr object. It may have a "default" attribute which indicates which subset should be selected by default. The selection of a subset of coefficients is performed by the select_coef function:

```
select_coef(bank_msq)
## (Intercept)
                     mktbk
                                 perfor
                                            dealdum
                                                           egrat
                                                                       optval
##
             1
                         2
                                      3
                                                   4
                                                                5
                                                                            6
##
     rho_eqrat
                rho_optval
             7
##
                          8
select_coef(bank_msq, subset = c("resid", "chol"))
                   rho_optval
                                  egrat/egrat
                                               optual/egrat optual/optual
##
       rho_eqrat
##
               7
                              8
                                            23
                                                          24
                                                                         25
```

select_coef is called inside the coef and the vcov methods for micsr objects:

```
coef(bank_msq)
##
     (Intercept)
                        mktbk
                                      perfor
                                                   dealdum
                                                                   egrat
## -3.0493980864 0.0007126479 4.6919607187
                                              0.8644131095 20.7983728258
##
                                 rho_optval
          optval
                    rho_eqrat
##
   0.0887552265 -0.4478945968 -0.1407430396
coef(bank_msq, subset = c("resid", "chol"))
                                 egrat/egrat optual/egrat optual/optual
##
       rho_egrat
                   rho_optval
     -0.44789460
                 -0.14074304
                                 56.80434859
                                             -0.01092933 0.14746163
##
vcov(bank_msq, subset = c("resid"))
##
                 rho_eqrat
                              rho_optval
## rho_eqrat
               0.0021818615 -0.0005167884
## rho_optval -0.0005167884 0.0045537894
```

Another way to select a subset of coefficients is to provide a regular expression for the grep argument. For example, to get all the coefficients that contains "Intercept":

```
vcov(bank_msq, subset = "all", grep = "Intercept")
##
                              (Intercept) instr_eqrat_(Intercept)
## (Intercept)
                             0.0026070311
                                                     -5.640990e-04
                                                      1.259446e-03
## instr eqrat (Intercept) -0.0005640990
## instr optval (Intercept) -0.0001772582
                                                     -2.817664e-20
                            instr_optval_(Intercept)
##
## (Intercept)
                                       -1.772582e-04
## instr_eqrat_(Intercept)
                                        -3.381197e-20
## instr optval (Intercept)
                                        1.259446e-03
```

The **npar** function extracts the number of the whole set of coefficients or of specific subsets:

```
npar(bank_msq)
## [1] 25
npar(bank_msq, subset = c("resid", "chol"))
## [1] 5
```

Estimating function, hessian and individual contribution to the log-likelihood

The estimating function is a $N \times K$ matrix containing the derivatives of the N elements of the likelihood function with respect to the K-lenght parameter vector. Its column-sum is the gradient that should be close to 0 at the optimum. The sandwich::estfun function is a generic that extract this information and several methods are provided for different objects. Some of these method are quite tedious as the matrix is not stored in the object containing the fitted models. For models of class micsr, this matrix is stored in the gradient element and the method is just: x\$gradient. This matrix is particularly useful to compute the variance-covariance matrix estimator based on the outer-product of the gradient or on sandwich formula.

The hessian is the $K \times K$ matrix of second-derivatives of the log-likelihood function with respect with the parameters vector. Its stored in the **hessian** object of a **micsr** object. In sandwich estimators of the covariance matrix, the "meat" is $N(-H)^{-1}$ and it is how the **meat** method for **micsr** objects is defined.

The information matrix is either the variance of the gradient or the opposite of the expectation of the hessian. When the analytical computation of the information matrix is possible, it is stored in the **info** element of the **micsr** object.

The log-likelihood is the sum of N contributions: the individual contributions is a N-length vector, which is stored as the **value** element of the **micsr** object. This vector is particularly

usefull to compute Vuong's test.

Covariance matrix estimation

Three elements of the object can be used to compute different flavors of the covariance matrix of the coefficients:

- gradient to compute the outer-product of the gradient estimator,
- hessian to compute the hessian-based estimator,
- info to compute the information-based estimator.

These matrix are computed using the vcov method, which has a vcov argument that can be set to "info", "hessian" or "opg".

```
vcov(bank_msq, subset = "resid", vcov = "opg")
```

rho_eqrat rho_optval rho_eqrat 0.0025591467 -0.0001606321 rho_optval -0.0001606321 0.0030387065

The vector of standard errors are often used, in particular in the table of coefficients. It can be obtained by taking the square root of the diagonal elements of the covariance matrix, or more simply by using micsr::stder.

```
sqrt(diag(vcov(bank_msq, subset = "resid")))
## rho_eqrat rho_optval
## 0.04671040 0.06748177
stder(bank_msq, subset = "resid")
## rho_eqrat rho_optval
## 0.04671040 0.06748177
```

Goodness of fit measures

For models fitted by maximum likelihood, most of the GOF statistics are based on the value of the objective function at the optimum. Three values of the log-likelihood are stored in the logLik element of a micsr object:

- the value at the optimum, for the fitted model,
- the value for the **saturated** model, i.e., the model with no degrees of freedom,
- the value for the **null** model, i.e., the model without any covariates.

Any of these values can be extracted using the logLik method, which has a type argument:

```
logLik(pbt)
## 'log Lik.' -318.7685 (df=4)
logLik(pbt, type = "model")
## 'log Lik.' -318.7685 (df=4)
logLik(pbt, type = "saturated")
## 'log Lik.' 0 (df=842)
logLik(pbt, type = "null")
## 'log Lik.' -370.666 (df=1)
```

Comparing fitted models using the value of the log-likelihood is not relevant because introducing more covariates (even if they are irrelevant) will necessarily increase the value of the log-likelihood. **AIC** and **BIC** are two information measures that take into account the number of fitted parameters. The formulas are respectively:

```
-2 ln L + kK
-2 ln L + K ln N
AIC(pbt)
## [1] 645.537
BIC(pbt)
## [1] 664.4802
AIC(pbt, type = "null")
## [1] 743.332
AIC(pbt, k = 5)
## [1] 657.537
```

The deviance is minus twice the difference between a model and the hypothetical saturated model. For a linear gaussian model, this is the sum of square residuals. The deviance method for micsr object has a type argument equal either to "model" (the default) or "null". In the latter case, we obtain the "null deviance":

```
deviance(pbt)
## [1] 637.537
deviance(pbt, type = "null")
## [1] 741.332
```

Finally, the relevance of a proposed model can be addressed using a test that "all the coefficients except the intercept are zero", which is the equivalent of the \mathbf{F} test for the linear regression model. Three tests can be conducted, either the Wald test, the score test and the likelihood ratio test. The values of the statistics are stored in the **test** element of the result:

pbt\$test ## wald score lr ## 80.74629 93.55961 103.79495

Summary

The summary method use the preceding infrastructure to compute the usual table of coefficients that contains the estimators, the standard errors, the statistics and the probability values. A subset of coefficients can be obtained using the subset argument and the covariance matrix is chosen using the vcov argument:

```
summary(bank_msq, subset = c("chol", "resid"), vcov = "opg")
```

```
Maximum likelihood estimation
```

```
Estimate Std. Error
                                      z-value Pr(>|z|)
rho_eqrat
             -0.44789460 0.05061637
                                      -8.8488
                                               < 2e-16 ***
rho_optval
             -0.14074304 0.05584664 -2.5202
                                               0.01173 *
eqrat | eqrat
             56.80434859 0.34566405 164.3340
                                               < 2e-16 ***
optval|egrat
             -0.01092933 0.00716298 -1.5258
                                               0.12706
optval|optval 0.14746163 0.00020104 733.4920 < 2e-16 ***
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
log-Likelihood: -902.15
```